

GATEFORUM Pioneers in Digital courses for GATE since 2008 has long history of training students through innovative courses. Currently GATEFORUM offers a wide range of courses from eGATE, GATE Online, Gdrive to Online TarGATE. Since inception, we have trained more 3,00,000 students since inception.

For more details visit gateforumonline.com

## General Aptitude

Q. No. 1-5 Carry One Mark Each

1. Writing too things on the $\qquad$ while teaching could make the students get $\qquad$ .
(A) board/board
(B) board/bored
(C) bored/board
(D) bored/bored

Answer:
(B)

## Click here to watch video explanation

2. Which one of the following is a representation (not to scale and in bold) of all values of $x$ satisfying the inequality $2-5 x \leq \frac{6 x-5}{3}$ on the real number line?
(A)
(B)


Answer:
(C)
3. If $f(x)=2 \ln \left(\sqrt{e^{x}}\right)$, what is the area bounded by $f(x)$ for the interval $[0,2]$ on the axis?
(A) 4
(B) $\frac{1}{2}$
(C) 1
(D) 2

Answer:
(C)

Click here to watch video explanation
4. A person was born on the fifth Monday of February in a particular year.

Which one of the following statements is correct based on the above information?
(A) The $2^{\text {nd }}$ February of that year is a Tuesday
(B) There will be five Sundays in the month of February in that year
(C) The $1^{\text {st }}$ February of that year is a Sunday
(D) All Mondays of February in that year have even dates

Answer: (A)
Click here to watch video explanation
5.


Which one of the groups given below can be assembled to get the shape that is shown above using each piece only one without overlapping with each other?
(rotation and translation operations may be used)
Answer:
(B OR C)
Click here to watch video explanation

## Q. No. 6 to 10 Carry Two Marks Each

6. Fish belonging to species $S$ in the deep sea have skins that area extremely black (ultra-black skin). This helps them not only to avoid predators but also sneakily attack their prey. However, having this extra layer of black pigment results in lower collagen on their skin, making their skin more fragile.
Which one of the following is the CORRECT logical inference based on the information in the above passage?
(A) Having ultra-black skin i sonly advantages to species S
(B) Having ultra-black skin has both advantages and disadvantages to species S
(C) Species S with lower collagen in their skin are at an advantage because it helps them avoid predators
(D) Having ultra-black skin is only disadvantageous to species S but advantageous only to their predators

Answer:
(C)

Click here to watch video explanation
7. For the past $m$ days, the average daily production at a company was 100 units per day.

If today's production of 180 unit changes the average to 110 units per day, what is the value of $m$ ?]
(A) 10
(B) 7
(C) 18
(D) 5

Answer
C)

Click here to watch video explanation
8. Consider the following functions for non-zeor positive integers, p and q .

(A) $f(3,2)>g(3,2)$
(B) $f(2,2)=g(2,2)$
(C) $\mathrm{g}(2,1) \neq \mathrm{f}(2,1)$
(D) $\mathrm{f}(\mathrm{g}(2,2), 2)<\mathrm{f}(2, \mathrm{~g}(2,2))$

Answer: (A)
Click here to watch video explanation
9. Four cities, P, Q, R and S are connected through one-way routes as shown in the figure. The travel time between any two connected cities is one hour. The boxes beside each city name describe the starting time of first train of the day and their frequency of operation. For example, from city P, the first trains of the day start at 8 AM with a frequency of 90 minutes to each of R and S . A person does not spend additional time at any city other than the waiting time for the next connecting train.

If the person starts from $R$ at 7 AM and is required to visit $S$ and return to $R$, what is the minimum time required?

(A) 5 hours 15 minutes
(C) 3 hours 45 minutes
(B) 4 hours 30 minutes
(D) 6 hours 30 minutes

Answer: (A)
Click here to watch video explanation
10. Equal sized circular regions are shaded in a square sheet of paper of 1 cm side length. Two cases, case M and case N , are considered as shown in the figures below. In the case M , four circles are shaded in the square sheet and in the case N , nine circles are shaded in the square sheet as shown.
What is the ratio of the areas of unshaded regions of case M to that of case N ?

case M

case M
(A) $2: 1$
(B) $2: 3$
(C) $1: 1$
(D) 3:2

Answer: (B)
Click here to watch video explanation

# Mechanical Engineering <br> Q. No. 11- 35 Carry One Mark Each 

11. $F(t)$ is a periodic square wave function as shown. It takes only two values, 4 and 0 , and stays at each of these values for 1 second before changing. What is the constant term in the Fourier series expansion of $\mathrm{F}(\mathrm{t})$ ?

(A) 2
(B) 1
(C) 4
(D) 3

Answer: (A)
12. Consider a cube of unit edge length and sides parallel to co-ordinate axes, with its centroid at the point $(1,2,3)$. The surface integral $\int_{A} \vec{F} \cdot d \vec{A}$ of a vector field $\vec{F}=3 x \hat{i}+5 y \hat{j}+6 z \hat{k}$ over the entire surface $A$ of the cube is $\qquad$ .
(A) 27
(B) 14
(C) 28
(D) 31

Answer:
(B) . . Click here to watch video explanation
13. Consider the definite integral

$$
\int_{1}^{2}\left(4 x^{2}+2 x+6\right) d x
$$

Let $I_{e}$ be the exact value of the integral. If the same integral is estimated using Simpson's rule with 10 equal subintervals, the value is $I_{s}$. The percentage error is defined as $e=100 \times\left(I_{e}-I_{s}\right) / I_{e}$. The value of $e$ is
(A) 3.5
(B) 0
(C) 2.5
(D) 1.2

Answer:
(B)

Click here to watch video explanation
14. Given $\int_{-\infty}^{\infty} \mathrm{e}^{-x^{2}} d x=\sqrt{\pi}$

If $a$ and $b$ are positive integers, the value of $\int_{-\infty}^{\infty} \mathrm{e}^{-\mathrm{a}(x+b)^{2}} \mathrm{dx}$ is $\qquad$ .
(A) $\sqrt{\pi a}$
(B) $\sqrt{\frac{\pi}{a}}$
(C) $\mathrm{b} \sqrt{\pi \mathrm{a}}$
(D) $\mathrm{b} \sqrt{\frac{\pi}{\mathrm{a}}}$

Answer:
(B)

Click here to watch video explanation
15. A polynomial $\psi(s)=a_{n} n^{n}+a_{n-1} s^{n-1}+\ldots .+a_{1} s+a_{0}$ of degree $n>3$ with constant real coefficients $a_{n}, a_{n-1}, \ldots . a_{0}$ has triple roots at $S=-\sigma$. Which one of the following conditions must be satisfied?
(A) $\psi(\mathrm{s})=0, \frac{\mathrm{~d} \psi(\mathrm{~s})}{\mathrm{ds}}=0$, and $\frac{\mathrm{d}^{2} \psi(\mathrm{~s})}{\mathrm{ds}^{2}}=0$ at $\mathrm{s}=-\sigma$
(B) $\psi(\mathrm{s})=0$, and $\frac{\mathrm{d}^{3} \psi(\mathrm{~s})}{\mathrm{ds}^{3}}=0$ at $\mathrm{s}=-\sigma$
(C) $\psi(s)=0$ at all three values of $s$ satisfying $\mathrm{s}^{3}+\sigma^{3}=0$
(D) $\psi(\mathrm{s})=0, \frac{\mathrm{~d}^{2} \psi(\mathrm{~s})}{\mathrm{ds}^{2}}=0$, and $\frac{\mathrm{d}^{4} \psi(\mathrm{~s})}{\mathrm{ds}^{4}}=0$ at $\mathrm{s}=-\sigma$

Answer: (A)
Click here to watch video explanation
16. Which one of the following is the definition of ultimate tensile strength (UTS) obtained from a stressstrain test on metal specimen?
(A) The maximum load attained divided by the original cross-sectional area
(B) Stress value where the stress-strain curve transitions from elastic to plastic behaviour
(C) The maximum load attained divided by the corresponding instantaneous cross-sectional area
(D) Stress where the specimen fractures

Answer: (A)
Click here to watch video explanation
17. A massive uniform rigid circular disc is mounted on a frictionless bearing at the end E of massive uniform rigid shaft AE which is suspended horizontally in a uniform gravitational field by two identical light extensible strings AB and CD as shown, where G is the center of mass of the shaft-disc assembly and $g$ is the acceleration due to gravity. The disc is then given a rapid spin $\omega$ about its axis in the positive x -axis direction as shown, while the shaft remains at rest. The direction of rotation is defined by using the right-hand thumb rule. If the string AB is suddenly cut, assuming negligible Energy dissipation, the shaft AE will

(A) rotate slowly (compared to $\omega$ ) about the positive $y$-axis direction
(B) rotate slowly (compared to $\omega$ ) about negative z -axis direction
(C) rotate slowly (compared to $\omega$ ) about the negative y-axis direction
(D) rotate slowly (compared to $\omega$ ) about the positive z -axis direction.

Answer: (B)
Click here to watch video explanation
18. A structural member under loading has a uniform state of plane stress which in usual notations is given by $\sigma_{x}=3 P, \sigma_{y}=-2 P$ and $\tau_{x y}=\sqrt{2} P$, where $P>0$. The yield strength of the material is 350 MPa . If the member is designed using the maximum distortion energy theory, then the value of P at which yielding starts (according to the maximum distortion energy theory) is
(A) 75 MPa
(B) 120 MPa
(C) 90 MPa
(D) 70 MPa

Answer: (D)
Click here to watch video explanation
19. Fluidity of a molten alloy during sand casting depends on its solidification range. The phase diagram of a hypothetical binary alloy of components A and B is shown in the figure with its eutectic composition and temperature. All the lines in this phase diagram, including the solidus and liquidus lines, are straight lines. If this binary alloy with 15 weight $\%$ of B is poured into a mould at a pouring temperature of 800
${ }^{\circ} \mathrm{C}$, then the solidification range is

(A) $400^{\circ} \mathrm{C}$
(B) $250^{\circ} \mathrm{C}$
(C) $150^{\circ} \mathrm{C}$
(D) $800^{\circ} \mathrm{C}$

Answer: (C)
Click here to watch video explanation
20. A shaft of diameter $25_{-0.074}^{-0.04} \mathrm{~mm}$ is assembled in a hole of diameter $25_{-0.00}^{+0.02} \mathrm{~mm}$. Match the allowance and limit parameter in Column I with its corresponding quantitative value in Column II for this shaft-hole assembly.

| Allowance and limit parameter (Column I) |  | Quantitative value (Column II) |  |
| :--- | :--- | :---: | :--- |
| $\mathbf{P}$ | Allowance | $\mathbf{1}$ | 0.09 mm |
| $\mathbf{Q}$ | Maximum clearance | $\mathbf{2}$ | 24.96 mm |
| $\mathbf{R}$ | Maximum material limit for hole | $\mathbf{3}$ | 0.04 mm |
|  |  | $\mathbf{4}$ | 25.0 mm |

(A) $\mathrm{P}-1, \mathrm{Q}-3, \mathrm{R}-2$
(B) $\mathrm{P}-3, \mathrm{Q}-1, \mathrm{R}-4$
(C) $\mathrm{P}-1, \mathrm{Q}-3, \mathrm{R}-4$
(D) $\mathrm{P}-3, \mathrm{Q}-1, \mathrm{R}-2$

Answer:
(B)

Click here to watch video explanation
21. Match the additive manufacturing technique in Column I with its corresponding input material in Column II.

| Additive manufacturing technique (Column I) |  | Input material (Column II) |  |
| :--- | :--- | :--- | :--- |
| $\mathbf{P}$ | Fused deposition modelling | $\mathbf{1}$ | Photo sensitive liquid resin |
| $\mathbf{Q}$ | Laminated object manufacturing | $\mathbf{2}$ | Heat fusible powder |
| $\mathbf{R}$ | Selective Laser sintering | $\mathbf{3}$ | Filament of polymer |
|  |  | $\mathbf{4}$ | Sheet of thermoplastic or <br> green compacted metal sheet |

(A) $\mathrm{P}-4, \mathrm{Q}-1, \mathrm{R}-4$
(B) $\mathrm{P}-3, \mathrm{Q}-4, \mathrm{R}-2$
(C) $\mathrm{P}-2, \mathrm{Q}-3, \mathrm{R}-1$
(D) $\mathrm{P}-1, \mathrm{Q}-2, \mathrm{R}-4$

Answer: (B)

## Click here to watch video explanation

22. Which one of the following CANNOT impart linear motion in a CNC machine?
(A) Linear motor
(B) Ball screw
(C) Lead screw
(D) Chain and sprocket

Answer: (D)
Click here to watch video explanation
23. Which one of the following is an intensive property of a thermodynamic system?
(A) Volume
(B) Mass
(C) Energy
(D) Density

Answer: (D)
Click here to watch video explanation
24. Consider a steady flow through a horizontal divergent channel, as shown in the figure, with supersonic flow at the inlet. The direction of flow is from left to right.


Pressure at location B is observed to be higher than that at an upstream location A.
Which among the flowing options can be the reason?
(A) Viscous effect
(B) Since volume flow rate is constant, velocity at B is lower than velocity at A
(C) Normal shock
(D) Boundary layer separation

Answer: (C)
Click here to watch video explanation
25. Which of the following non-dimensional terms is an estimate of Nusselt number?
(A) Ratio of the rate at which internal energy is advected to the rate of conduction heat transfer
(B) Non-dimensional temperature gradient
(C) Ratio of internal thermal resistance of a solid to the boundary layer thermal resistance
(D) Non-dimensional velocity gradient multiplied by Prandtl number

Answer: (B)
Click here to watch video explanation
26. A square plate is supported in four different ways (configurations $(\mathrm{P})$ to ( S ) as shown in the figure). A couple moment C is applied on the plate. Assume all the members to be rigid and mass-less, and all joints to be frictionless. All support links of the plate are identical.
(P)

(Q)

(R)

(S)


The square plate can remain in equilibrium in its initial state for which one or more of the following support configurations?
(A) Configuration (P)
(B) Configuration (R)
(C) Configuration (Q)
(D) Configuration (S)

Answer:
(B, C, D)
Click here to watch video explanation
27. Consider sand casting of a cube of edge length a. A cylindrical riser is placed at the top of the casting. Assume solidification time, $\mathrm{t}_{\mathrm{s}} \propto \mathrm{V} / \mathrm{A}$, where V is the volume and A is the total surface area dissipating heat. If the top of the riser is insulated, which of the following radius/radii of riser is/are acceptable?
(A) $\frac{\mathrm{a}}{4}$
(B) $\frac{\mathrm{a}}{2}$
(C) $\frac{\mathrm{a}}{3}$
(D) $\frac{\mathrm{a}}{6}$

Answer: (B, C)
Click here to watch video explanation
28. Which of these processes involve(s) melting in metallic workpieces?
(A) Laser beam machining
(B) Electron beam machining
(C) Electrochemical machining
(D) Electric discharge machining

Answer:
(A, B, D)
Click here to watch video explanation
29. The velocity field in a fluid is given to be $\vec{V}=(4 x y) \hat{i}+2\left(x^{2}-y^{2}\right) \hat{j}$

Which of the following statements(s) is/are correct?
(A) The velocity field is one-dimensional.
(B) The flow is incompressible.
(C) The acceleration experienced by a fluid particle is zero at $(x=0, y=0)$.
(D) The flow is irrotational.

Answer:
(B, C, D)
Click here to watch video explanation
30. A rope with two mass-less platforms at its two ends passes over a fixed pulley as shown in the figure. Discs with narrow slots and having equal weight of 20 N each can be placed on the platforms. The number of discs placed on the left side platform is n and that on the right side platform is M .

It is found that for $\mathrm{n}=5$ and $\mathrm{m}=0$, force $\mathrm{F}=200 \mathrm{~N}$ (refer to part (i) of the figure) is just sufficient to initiate upward motion of the left side platform. If the force F is removed, then the minimum value of m (refer to part (ii) of the figure) required to prevent downward motion of the left side platform is $\qquad$ (in integer).


Answer: (3 to 3)

Click here to watch video explanation
31. For a dynamical system governed by the equation,

$$
\ddot{\mathrm{x}}(\mathrm{t})+\mathrm{z} \xi \omega_{\mathrm{n}} \dot{\mathrm{x}}(\mathrm{t})+\omega_{\mathrm{n}}^{2} \mathrm{x}(\mathrm{t})=0
$$

The damping ratio $\xi$ is equal to $\frac{1}{2 \pi} \log _{\mathrm{e}} 2$. The displacement x of this system is measured during a hammer test. A displacement peak in the positive displacement direction is measured to be 4 mm . Neglecting higher powers ( $>1$ ) of the damping ratio, the displacement at the next peak in the positive displacement direction is measured to be 4 mm . Neglecting higher powers ( $>1$ ) of the damping ratio, the displacement at the next peak in the positive direction will be $\qquad$ mm (in integer).
Answer:
( 1.95 to 2.05)
Click here to watch video explanation
32. An electric car manufacturer underestimated the January sales of car by 20 units, while the actual sales was 120 units. If the manufacturer uses exponential smoothing method with smoothing constant of $\alpha=0.2$, then the sales forecast for the month of February of the same year is $\qquad$ units (in integer).

Answer:
(104 to 104)
Click here to watch video explanation
33. The demand of a certain part is 1000 parts/year and its cost is Rs. 1000 /part. The orders are paced based on the economic order quantity (EOQ). The cost of ordering is Rs.100/order and the lead time for receiving the order is 5 days. If the holding cost is Rs.20/part/year, the inventory level for placing the order is $\qquad$ parts (round off to the nearest integer).

Answer:
(13 to 15)
Click here to watch video explanation
34. Consider 1 kg of an ideal gas at 1 bar and 300 K contained in a rigid and perfectly insulated container. The specific heat of the gas at constant volume $\mathrm{c}_{\mathrm{v}}$ is equal to $750 \mathrm{~J} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~K}^{-1}$ A stirrer performs 225 kJ of the work on the gas. Assume that the container does not participate in the thermodynamic interaction. The final pressure of the gas will be $\qquad$ bar (in integer).

Answer: (2 to 2) Click here to watch video explanation


For more details visit gateforumonline.com
35. Wien's law is stated as follows; $\lambda_{\mathrm{m}} \mathrm{T}=\mathrm{C}$, where C is $2898 \mu \mathrm{~m} . \mathrm{K}$ and $\lambda_{\mathrm{m}}$ is the wavelength at which the emissive power of a black body is maximum for a given temperature T. The spectral hemispherical emissivity $\left(\varepsilon_{\lambda}\right)$ of a surface is shown in the figure below $\left(1 \AA=10^{-10} \mathrm{~m}\right)$. The temperature at which the total hemispherical emissivity will be highest is $\qquad$ $K$ (round off to the nearest integer).


Answer: (4825 to 4835)
Click here to watch video explanation

## O.No. 36-65 Carry Two Marks Each

36. For the exact differential equation,

$$
\frac{\mathrm{du}}{\mathrm{dx}}=\frac{-\mathrm{xu}^{2}}{2+\mathrm{x}^{2} \mathrm{u}},
$$

Which one of the following is the solution?
(A) $\mathrm{u}^{2}+2 \mathrm{x}^{2}=$ constant
(B) $\frac{1}{2} \mathrm{ux}^{2}+2 \mathrm{x}=$ constant
(C) $\frac{1}{2} x^{2} u^{2}+2 u=$ constant
(D) $\mathrm{xu}^{2}+\mathrm{u}=$ constant

Answer:
(C)
37. A rigid homogenous uniform block of mass 1 kg , height $\mathrm{h}=0.4 \mathrm{~m}$ and width $\mathrm{b}=0.3 \mathrm{~m}$ is pinned at one corner and placed upright in a uniform gravitational field ( $\mathrm{g}=9.81 \mathrm{~m} / \mathrm{s}^{2}$ ), supported by a roller in the configuration shown in the figure. A short duration (impulsive) force F , producing an impulse $\mathrm{I}_{\mathrm{F}}$ is applied at a height of $\mathrm{d}=0.3 \mathrm{~m}$ from the bottom as shown. Assume all joints to be frictionless, The minimum value of $\mathrm{I}_{\mathrm{F}}$ required to topple the block is

(A) 1.172 Ns
(B) 0.814 Ns
(C) 0.953 Ns
(D) 1.403 Ns

Answer: (C)
Click here to watch video explanation
38. A linear elastic structure under plane stress condition is subjected to two sets of loading I and II. The resulting states of stress at a point corresponding to these two loadings are as shown in the figure below. If these two sets of loading are applied simultaneously, then the net normal component of stress $\sigma_{x x}$ is
$\qquad$ —.


Loading - I


Loading - II
(A) $3 \sigma / 2$
(B) $\sigma(1-1 / \sqrt{2})$
(C) $\sigma(1+1 \sqrt{2})$
(D) $\sigma / 2$

Answer: (A)
Click here to watch video explanation
39. A rigid body in the $\mathrm{X}-\mathrm{Y}$ plane consists of two point masses ( 1 kg each) attached to the end of two mass less rods, each of 1 cm length, as shown in the figure. It rotates at 30 RPM counter-clockwise about the Z-axis passing through point O . A point mass of $\sqrt{2} \mathrm{~kg}$, attached to one end of a third massless rod, is used for balancing the body by attaching the free end of the rod to point O . The length of the third rod is $\qquad$ cm
$\qquad$
(A) 1
(B) $1 / 2 \sqrt{2}$
(C) $1 / \sqrt{2}$
(D) $\sqrt{2}$

Answer: (A)


Click here to watch video explanation
40. A spring mass damper system (mass $m$, stiffness $k$, and damping coefficient c ) excited by a force $\mathrm{F}(\mathrm{t})=$ $B \sin \omega \mathrm{t}$, where $\mathrm{B}, \omega$ and t are the amplitude, frequency and time, respectively, is shown in the figure. Four different responses of the system (marked as (i) to (iv)) are shown just to the right of the system figure. In the figures of the responses, A is the amplitude of response shown in red color and the dashed lines indicates its envelope. The responses represent only the quantitative trend and those are not drawn to any specific scale.


Four different parameter and forcing conditions are mentioned below.
(P) $\mathrm{c}>0$ and $\omega=\sqrt{\mathrm{k} / \mathrm{m}}$
(Q) $\mathrm{c}<0$ and $\omega \neq 0$
(D) $\mathrm{c}=0$ and $\omega=\sqrt{\mathrm{k} / \mathrm{m}}$
(S) $\mathrm{c}=0$ and $\omega \cong \sqrt{\mathrm{k} / \mathrm{m}}$

Which one of the following options gives correct match (indicated by arrow $\rightarrow$ ) of the parameter and forcing conditions to the responses?
(A) (P) $\rightarrow$ (ii), (Q) $\rightarrow$ (iii), (R) $\rightarrow$ (iv), (S) $\rightarrow$ (i)
(B) (P) $\rightarrow$ (i), (Q) $\rightarrow$ (iii), (R) $\rightarrow$ (iv), (S) $\rightarrow$ (ii)
(C) (P) $\rightarrow$ (i), (Q) $\rightarrow$ (iv), (R) $\rightarrow$ (ii), (S) $\rightarrow$ (iii)
(D) (P) $\rightarrow$ (iii), (Q) $\rightarrow$ (iv), (R) $\rightarrow$ (ii), (S) $\rightarrow$ (i)

Answer: (C)
Click here to watch video explanation
41. Parts P1-P7 are machined first on a milling machine and then polished at a separate machine. Using the information in the following table, the minimum total completion time required for carrying out both the operations for all 7 parts is $\qquad$

| Part | Milling(hours) | Polishing (hours) |
| :---: | :---: | :---: |
| P1 | 8 | 6 |
| P2 | 3 | 2 |
| P3 | 3 | 4 |
| P4 | 4 | 6 |
| P5 | 5 | 7 |
| P6 | 6 | 4 |
| P7 | 2 | 1 |

(A) 33
(B) 32
(C) 31
(D) 30

Answer: (A)
42. A manufacturing unit produces two products P1 and P2. For each piece of P1 and P2, the table blow provides quantities of material M1, M2, and M3 required, and also the profit earned. The maximum quantity available per day for M1, M2 and M3 is also provided. The maximum possible profit per day is Rs $\qquad$ .

|  | M1 | M2 | M3 | Profit per piece (Rs) |
| :---: | :---: | :---: | :---: | :---: |
| P1 | 2 | 2 | 0 | 150 |
| P2 | 3 | 1 | 2 | 100 |
| Maximum <br> quantity <br> available per day | 70 | 50 | 40 |  |

(A) 4000
(B) 6000
(C) 5000
(D) 3000

Answer:
(A)
43. A tube of uniform diameter D is immersed in a steady flowing inviscid liquid stream of velocity V , as shown in the figure. Gravitational acceleration is represented by g . The volume flow rate through the tube is $\qquad$ .

(A) $\frac{\pi}{4} D^{2} V$
(B) $\frac{\pi}{4} \mathrm{D}^{2} \sqrt{2 \mathrm{~g}\left(\mathrm{~h}_{1}+\mathrm{h}_{2}\right)}$
(C) $\frac{\pi}{4} \mathrm{D}^{2} \sqrt{2 \mathrm{gh}_{2}}$
(D) $\frac{\pi}{4} \mathrm{D}^{2} \sqrt{\mathrm{~V}^{2}-2 \mathrm{gh}_{2}}$

Answer: (D)
Click here to watch video explanation
44. The steady velocity field in an inviscid fluid of density 1.5 is given to be $\vec{V}=\left(y^{2}-x^{2}\right) \hat{i}+(2 x y) \hat{j}$. Neglecting body forces, the pressure gradient at $(x=1, y=1)$ is $\qquad$ .
(A) $10 \hat{\mathrm{j}}$
(B) $20 \hat{\mathrm{i}}$
(C) $-6 \hat{\mathrm{i}}-6 \hat{\mathrm{j}}$
(D) $-4 \hat{\mathrm{i}}-4 \hat{\mathrm{j}}$

Answer:
(C)

Click here to watch video explanation
45. In a vapour compression refrigeration cycle, the refrigerant enters the compressor in saturated vapour state at evaporator pressure, with specific enthalpy equal to $250 \mathrm{~kJ} / \mathrm{kg}$. The exit of the compressor is superheated at condenser pressure with specific enthalpy equal to $300 \mathrm{~kJ} / \mathrm{kg}$. At the condenser exit, the refrigerant is throttled to the evaporator pressure. The coefficient of performance (COP) of the cycle is 3 . If the specific enthalpy of the saturated liquid at evaporator pressure is $50 \mathrm{~kJ} / \mathrm{kg}$, then the dryness fraction of the refrigerant at entry to evaporator is $\qquad$ .
(A) 0.2
(B) 0.3
(C) 0.35
(D) 0.25

Answer:
(D)

Click here to watch video explanation
46. $A$ is a $3 \times 5$ real matrix of rank 2 . For the set of the homogeneous equations $A x=0$, where 0 is a zero vector and $x$ is vector of unknown variable, which of the flowing is/are true?
(A) The given set of equations will be satisfied by a zero vector of appropriate size.
(B) The given set of equations will have infinitely many solutions.
(C) The given set of equations will have a unique solution.
(D) The given set of equations will have many but a finite number of solutions.

Answer: (A, B)

Click here to watch video explanation
47. The lengths of members BC and CE in the frame shown in the figure are equal. All the members are rigid and lightweight, and the friction at the joints is negligible. Two forces of magnitude $\mathrm{Q}>0$ are applied as shown, each at the mid-length of the respective member on which it acts.


Which one or more of the following members do not carry any load (force)?
(A) AB
(B) GH
(C) CD
(D) EF

Answer:
(B, C)
Click here to watch video explanation
48. If the sum and product of eigen values of $2 \times 2$ real matrix $\left[\begin{array}{ll}3 & p \\ p & q\end{array}\right]$ are 4 and -1 respectively, the $|p|$ is
$\qquad$ (in integer).
Answer:
(2 to 2)
Click here to watch video explanation
49. Given $\mathrm{z}=\mathrm{x}+\mathrm{iy}, \mathrm{i}=\sqrt{-1} . \mathrm{C}$ is a circle of radius 2 with the centre at the origin. If the contour C is traversed anticlockwise, then the value of the integral $\frac{1}{2 \pi} \int_{C} \frac{1}{(z-i)(z+4 i)} \mathrm{dz}$ is ___ (round off to one decimal place).

Answer:
(0.2 to 0.2)

Click here to watch video explanation
50. A shaft of length $L$ is made of two materials, one in the inner core and the other in the outer rim, and the two are perfectly joined together (no slip at the interface) along the entire length of the shaft. The diameter of the inner core is $d_{i}$ and the external diameter of the rim is $d_{0}$, as shown in the figure. The modulus of rigidity of the core and rim materials are $G_{i}$ and $G_{0}$, respectively. It is given that $d_{0}=2 d_{i}$ and $G_{i}=3 G_{0}$. When the shaft is twisted by application of a torque along the shaft axis, the maximum shear stress developed in the outer rim and the inner core turn out to be $\tau_{0}$ and $\tau_{\mathrm{i}}$, respectively. All the deformations are in the elastic range and stress strain relations are linear. Then the ratio $\tau_{\mathrm{i}} / \tau_{0}$ is ____(round off to 2 decimal places).


Shaft cross section
51. A rigid beam $A D$ of length $3 \mathrm{a}=6 \mathrm{~m}$ is hinged at frictionless pin joint A and supported by two strings as shown in the figure. String BC passes over two small frictionless pulleys of negligible radius. All the strings are made of the same material and have equal cross-section area. A force $\mathrm{F}=9 \mathrm{kN}$ is applied at C and the resulting stresses in the strings are within linear elastic limit. The self-weight of the beam is negligible with respect to the applied load. Assuming small deflections, the tension developed in the string at C is $\qquad$ kN (round off to 2 decimal places).

Answer: (1.48 to 1.52)

52. In the configuration of the planar four-bar mechanism at a certain instant as shown in the figure, the angular velocity of the 2 cm long link is $\omega_{2}=5 \mathrm{rad} / \mathrm{s}$. Given the dimensions as shown, the magnitude of the angular velocity $\omega_{4}$ of the 4 cm long link is given by $\qquad$ $\mathrm{rad} / \mathrm{s}($ round off to 2 decimal places).

53. A shaft AC rotating at a constant speed carries a thin pulley of radius $r=0.4 \mathrm{~m}$ at the end C which drives a belt. A motor is coupled at the end $A$ of the shaft such that it applies a torque $M_{z}$ about the shaft axis without causing any bending moment. The shaft is mounted on narrow frictionless bearings at A and B where $\mathrm{AB}=\mathrm{BC}=\mathrm{L}=0.5 \mathrm{~m}$. The taut and slack side tensions of the belt are $\mathrm{T}_{1}=300 \mathrm{~N}$ and $\mathrm{T}_{2}=100 \mathrm{~N}$, respectively. The allowable shear stress for the shaft material is 80 MPa . The self-weights of the pulley and the shaft are negligible. Use the value of $\pi$ available in the on-screen virtual calculator. Neglecting shock and fatigue loading and assuming maximum shear stress theory, the minimum required shaft diameter is $\qquad$ mm (round off to 2 decimal places).

Answer: (23.60 to 24.20)

------
Click here to watch video explanation
54. A straight-teeth horizontal slab milling cutter is shown in the figure. It has 4 teeth and diameter (D) of 200 mm . The rotational speed of the cutter is 100 rpm and the linear feed given to the work piece is 1000 $\mathrm{mm} / \mathrm{minute}$. The width of the work piece (w) is 100 mm , and the entire width is milled in a single pass of the cutter. The cutting force/tooth is given by $\mathrm{F}=\mathrm{Kt}_{\mathrm{c}} \mathrm{w}$, where specific cutting force $\mathrm{K}=10 \mathrm{~N} / \mathrm{mm}^{2}$, w is the width of cut, and $\mathrm{t}_{\mathrm{c}}$ is the uncut chip thickness.

The depth of cut (d) is D/2, and hence the assumption of $\frac{d}{D} \ll 1$ is invalid. The maximum cutting force required is $\qquad$ kN (round off to one decimal place).


Answer:
55. In an orthogonal machining operation, the cutting and thrust forces are equal in magnitude. The uncut chip thickness is 0.5 mm and the shear angle is $15^{\circ}$. The orthogonal rake angle of the tool is $0^{\circ}$ and the width of cut is 2 mm . The work piece material is perfectly plastic and its yield shear strength is 500 MPa . The cutting force is $\qquad$ N (round off to the nearest integer).

Answer:
(2700 to 2750)
Click here to watch video explanation
56. The best size wire is fitted in a groove of a metric screw such that the wire touches the flanks of the thread on the pitch line as shown in the figure. The pitch (p) and included angle of the thread are 4 mm and $60^{\circ}$, respectively. The diameter of the best size wire is $\qquad$ mm (round off to 2 decimal places).


Answer:
(2.29 to 2.33)

Click here to watch video explanation
57. In a direct current arc welding process, the power source has an open circuit voltage of 100 V and short circuit current of 1000 A . Assume a linear relationship between voltage and current. The arc voltage (V) varies with the arc length (l) as $\mathrm{V}=10+51$, where V is in volts and l is in mm . The maximum available arc power during the process is $\qquad$ kVA (in integer).

Answer:
( 25 to 25)
58. A cylindrical billet of 100 mm diameter and 100 m length is extruded by a direct extrusion process to produce a bar of L-section. The cross sectional dimensions of this L-section bar are shown in the figure. The total extrusion pressure (p) is MPa for the above process is related to extrusion ratio (r) as

$$
\mathrm{p}=\mathrm{K}_{\mathrm{s}} \sigma_{\mathrm{m}}\left[0.8+1.5 \ln (\mathrm{r})+\frac{21}{\mathrm{~d}_{\mathrm{o}}}\right],
$$

Where $\sigma_{\mathrm{m}}$ is the mean flow strength of the billet material in $\mathrm{MPa}, 1$ is the portion of the billet length remaining to be extruded in $m m, d_{0}$ is the initial diameter of the billet in $m m$, and $K_{s}$ is the die shape factor.


If the mean flow strength of the billet material is 50 MPa and the die shape factor is 1.05 , then the maximum force required at the start of extrusion is $\qquad$ kN
(round off to one decimal place).
Answer: (2426.0 to 2432.0)
59. A project consists of five activities (A, B, C, D and E). The duration of each activity follows beta distribution. The three time estimates (in weeks) of each activity and immediate predecessor(s) are listed in the table. The expected time of the project completion is $\qquad$ weeks (in integer).

| Activity | Time estimates (in weeks) |  |  | Immediate |
| :---: | :---: | :---: | :---: | :---: |
|  | Most likely <br> Time | Pessimistic <br> Time | predecessor(s) |  |
| A | 4 | 5 | 6 | None |
| B | 1 | 3 | 5 | A |
| C | 1 | 2 | 3 | A |
| D | 2 | 4 | 6 | C |
| E | 3 | 4 | 5 | B, D |

Answer:
( 15 to 15)
Click here to watch video explanation
60. A rigid tank of volume of $8 \mathrm{~m}^{3}$ is being filled up with air from a pipeline connected through a valve. Initially the valve is closed and the tank is assumed to be completely evacuated. The air pressure and temperate inside the pipeline are maintained at 600 kPa and 306 K , respectively. The filling of the tank begins by opening the valve and the process ends when the tank pressure is equal to the pipeline pressure. During the filling process, heat loss to the surrounding is 1000 kJ . The specific heats of air at constant pressure and at constant volume are $1.005 \mathrm{~kJ} / \mathrm{kg} . \mathrm{K}$ and $0.718 \mathrm{~kJ} / \mathrm{kg} . \mathrm{K}$, respectively. Neglect changes in kinetic energy and potential energy.

The final temperature of the tank after the completion of the filling process is $\qquad$ K (round off to the nearest integer).

Answer:
( 385 to 405)
Click here to watch video explanation
61. At steady state, $500 \mathrm{~kg} / \mathrm{s}$ of steam enters a turbine with specific enthalpy equal to $3500 \mathrm{~kJ} / \mathrm{kg}$ and specific entropy equal to $6.5 \mathrm{kJgg}^{-1} \cdot \mathrm{~K}^{-1}$. It expands reversibly in the turbine to the condenser pressure. Heat loss occurs reversibly in the turbine at a temperature of 500 K . If the exit specific enthalpy and specific entropy are $2500 \mathrm{~kJ} / \mathrm{kg}$ and $6.3 \mathrm{~kJ} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~K}^{-1}$, respectively, the work output from the turbine is
$\qquad$ MW (in integer).

Answer:
(450 to 450)
Click here to watch video explanation
62. A uniform wooden rod (specific gravity $=0.6$, diameter $=4 \mathrm{~cm}$ and length $=8 \mathrm{~m}$ ) is immersed in the water and is hinged without friction at point A on the waterline as shown in the figure. A solid spherical ball made of lead (specific gravity $=11.4$ ) is attached to the free end of the rod to keep the assembly in static equilibrium inside the water. For simplicity, assume that the radius of the ball is much smaller than the length of the rod.

Assume density of water $=10^{3} \mathrm{~kg} / \mathrm{m}^{3}$ and $\pi=3.14$
Radius of the ball is $\qquad$ cm (round off to 2 decimal places).


Answer:
(3.48 to 3.70 )
63. Consider steady state, one-dimensional heat conduction in an infinite slab of thickness 2 L ( $\mathrm{L}=1 \mathrm{~m}$ ) as shown in the figure. The conductivity ( k ) of the material varies with temperature as $\mathrm{k}=\mathrm{CT}$, where T is the temperature in K , and C is an constant equal to $2 \mathrm{~W} \mathrm{~m}^{-1} \cdot \mathrm{~K}^{-2}$. There is uniform heat generation of $1280 \mathrm{~kW} / \mathrm{m}^{3}$ in the slab. If both faces of the slab are maintained at 600 K , then the temperature at $\mathrm{x}=0$ is $\qquad$ $K$ (in integer).


Answer: (1000 to 1000)
Click here to watch video explanation
64. Saturated vapor at $200^{\circ} \mathrm{C}$ condenses to saturated liquid at the rate of $150 \mathrm{~kg} / \mathrm{s}$ on the shell side of a heat exchanger (enthalpy of condensation $\mathrm{h}_{\mathrm{fg}}=2400 \mathrm{~kJ} / \mathrm{kg}$ ). A fluid with $\mathrm{c}_{\mathrm{p}}=4 \mathrm{~kJ} \cdot \mathrm{~kg}^{-1} \cdot \mathrm{~K}^{-1}$ enters at $100^{\circ} \mathrm{C}$ on the tube side. If the effectiveness of the heat exchanger is 0.9 , then the mass flow rate of the fluid in the tube side is $\qquad$ $\mathrm{kg} / \mathrm{s}$ (in integer)

Answer: (1000 to 1000)
Click here to watch video explanation
65. Consider a hydrodynamically and thermally fully-developed, steady fluid flow of $1 \mathrm{~kg} / \mathrm{s}$ in a uniformly heated pipe with diameter of 0.1 m and length of 40 m . A constant heat flux of magnitude $15000 \mathrm{~W} / \mathrm{m}^{2}$ is imposed on the outer surface of the pipe. The bulk-mean temperature of the fluid at the entrance to the pipe is $200^{\circ} \mathrm{C}$. The Reynolds number (Re) of the flow is 85000 , and the Prandtl number ( Pr ) of the fluid is 5 . The thermal conductivity and the specific heat of the fluid are $0.08 \mathrm{~W} \cdot \mathrm{~m}^{-1} \cdot \mathrm{~K}^{-1}$ and $2600 \mathrm{~J} \cdot \mathrm{~kg}^{-1} \mathrm{~K}^{-1}$. respectively. The correlation $\mathrm{Nu}=0.023 \operatorname{Re}^{0.8} \mathrm{Pr}^{0.4}$ is applicable, where the Nusselt Number $(\mathrm{Nu})$ is defined on the basis of the pipe diameter. The pipe surface temperature at the exit is $\qquad$ ${ }^{\circ} \mathrm{C}$ (round off to the nearest integer).

Answer: (317 to 324)
Click here to watch video explanation


## Follow us @


@gateforum


For more details visit gateforumonline.com

